

Aufgabe 7

30.11.10

Notiztitel

Mathematical Gauge Theory WS 10/11

Let $M = \mathbb{S}^2$ the two-sphere as a submanifold of \mathbb{R}^3 and consider the Riemannian metric on $T\mathbb{S}^2$ induced by the standard euclidean metric of \mathbb{R}^3 . Let D be the Levi-Civita connection on $TM \rightarrow M$.

- a) Describe the Christoffel symbols and the geodesic equation explicitly with respect to local coordinates (e.g. stereographic projection).
- b) Show that the great circles are the geodesics.
- c) Determine the parallel transport $T_N M \rightarrow T_M M$ along geodesic triangles. It is a rotation with respect to an angle which is given by the triangle's data.
- d) Determine the holonomy group $G(N)$.
- e) Determine the curvature operator F .
- f) Discuss the corresponding case $\mathbb{S}^n \subset \mathbb{R}^{n+1}$.