A cusp

$$f(X, Y) = Y^2 - X^3 = 0$$

$$\frac{\partial f}{\partial X}(0,0) = 0 = \frac{\partial f}{\partial Y}(0,0)$$