

Tutorial in Mathematical Gauge Theory

Exercise 2

2. (a) Examine, whether or not the fibrations $TS^n \rightarrow S^n$ are trivial for $n = 1, 2, 3$.
- (b) Give a detailed description of the tautological bundle $T \rightarrow \mathbb{C}P^n$ (by bundle charts), where $T := \{(p, z) \in \mathbb{C}P^n \times \mathbb{C}^{n+1} \mid z = 0 \vee z \in p\} \subset \mathbb{C}P^n \times \mathbb{C}^{n+1}$ with the induced structure. Show that T is not trivial.