

**Problem set for
Advanced Algebra**

- (45) (a) Let $A\text{-Mod}$ be equivalent to $B\text{-Mod}$. Show that $\text{Mod-}A$ and $\text{Mod-}B$ are also equivalent.
(b) Let \mathbb{K} be an integral domain (commutative without zero-divisors). Show that $\mathbb{K}\text{-Mod} \simeq \text{Mod-}\mathbb{K}$.
- (46) Show that an equivalence of arbitrary categories preserves monomorphisms.
- (47) Show that an equivalence of module categories preserves projective modules, but not free modules.
- (48) Let D be a division algebra. Show that $D\text{-Mod} \simeq \text{Mod-}D$ if and only if there is an isomorphism of algebras $D \cong D^{op}$.

Due date: Tuesday, 22.1.2002, 16:15 in Lecture Hall 138