# word2vec <br> Mathematics and Applications of Machine Learning 

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## Structure

(1) What is it?
(2) Why do we need it?

- Alternatives
(3) Easy version
- Conceptual
- Code

4 General version

- CBOW
- Skip-gram
- Comparison
- Improvements
(5) Google's model


## What is word2vec/word embedding?

## The paper



Figure 1: Original paper by Mikolov et al.

- Two 2013 papers accumulating over 7000 citations.


## The task

Lorem ipsum dolor sit
amet, consetetur
sadipscing elitr, sed
diam nonumy eirmod
tempor invidunt ut
labore et dolore magna

## Corpus C

## The task



## The task

| Lorem ipsum dolor sit |
| :--- |
| amet, consetetur |
| sadipscing elitr, sed |
| diam nonumy eirmod |
| tempor invidunt ut |
| labore et dolore magna |

## Corpus C



$$
\begin{aligned}
& {[\text { lorem }=(0.1,0.4, \ldots, 0.3)} \\
& {[\text { ipsum }]=(2,0.5, \ldots, 0)}
\end{aligned}
$$



## Vector Space

Why do we want a word embedding algorithm?

## Main uses

- Classification.
- Sentence or document analysis.d
- Similarity analysis.

word_vectors.similarity('love', 'adore')
>>0. 681687380259
word_vectors.similarity('love', 'admire')
>>0. 490552324418
word_vectors.similarity('adore', 'admire')
>>0.637308353311


## Semantic networks

| en natural language |  |  | Documentation | FAQ | Chat | Blog |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| An English term in Concept |  |  |  |  |  |  |
|  View this term in the Apt |  |  |  |  |  |  |
| Synonyms | Types of natural language | Related terms | Links to ot | er sit |  |  |
| 14．自然言語 ${ }^{(a)}$ | －Afroasiatic ${ }^{(m)}$ | Enelve | swepencyecren Natu | ILang |  |  |
| ［ill Lingua Natural ${ }^{(n)+}$ | －n Amerind ${ }^{(n)}$－ | © prirozeny jazyk ${ }^{(0)}$－ | umbelarg Natura | nguag |  |  |
| dif naturliche sprache－ | －n Austro－Asiatic ${ }^{(m)}$ | en human－ | werdree－relt princeton | 10691 | －7－n |  |
| － as $^{(m)}$ | －m Austronesian ${ }^{(n)}$－ | －${ }^{\text {arirspeak }}{ }^{(n)}$ | enwikionuryerg na | al lang | e |  |
|  | En Basque ${ }^{(n)}$－ | Enatisymmetry ${ }^{(\mathrm{n})}$ |  |  |  |  |
|  | en Caucasian ${ }^{(n)}$ | m language |  |  |  |  |
| a idioma ${ }^{(n)}$ | m Chukchi language ${ }^{(n)}$ | en categorial grammar ${ }^{(0)}$ |  |  |  |  |
| ［1llengua ${ }^{(n)}$ | en Dravidian ${ }^{(n)}+$ | en natural－ |  |  |  |  |
| －llengua natural ${ }^{(n)} \rightarrow$ | en Elamitic ${ }^{(n)}+$ | －computational linguistics ${ }^{(0)}$－ |  |  |  |  |
| llenguatge natural ${ }^{(r)}$ | en Eskimo－Aleut ${ }^{(\mathrm{n})}$－ | en programming language－ |  |  |  |  |
| $\text { das sprog }{ }^{(n)}$ | tn Hmong language ${ }^{(n)}$ | n constructed language ${ }^{(n)}$ |  |  |  |  |
| tongue ${ }^{(n)}$ | －n Indo－European ${ }^{(n)}+$ | en high level ${ }^{(3)}$ |  |  |  |  |
| er idioma ${ }^{(n)}$－ | Enhoisan ${ }^{(\mathrm{n})}$ | m indexing language <br> en language isolate ${ }^{(m)}$ |  |  |  |  |
| as lengua ${ }^{(n)}$ | m mother tongue ${ }^{(n)}$ | m montague grammar（ n ）－ |  |  |  |  |
| ta venb $3^{4} 5^{(n)}$ | －n ${ }^{\text {Niger－Kordofanian }}{ }^{(n)}$ | en reification ${ }^{(\mathrm{n})}$ |  |  |  |  |
| $\mathrm{n}^{\text {¢ }}$ kieli ${ }^{(n)}$－ | en Nilo－Saharan ${ }^{(\mathrm{n})}$ | en seaspeak ${ }^{(0)}+$ |  |  |  |  |
| （t）langue ${ }^{(\mathrm{r})}-$ | en Papuan ${ }^{(n)}+$ | en sentiment analysis ${ }^{(m)}$－ |  |  |  |  |
| ［f．langue ethnique ${ }^{(t)}+$ | －n Sino－Tibetan ${ }^{(n)}+$ | n sign language ${ }^{(n)}+$ |  |  |  |  |
| Ffr langue naturelle ${ }^{(n)} \rightarrow$ | －m tone language ${ }^{(0)}$ | en transformational grammar ${ }^{(0)}$ ． |  |  |  |  |
| it lingua ${ }^{(n)}+$ | More＊ | More，${ }^{\text {a }}$ |  |  |  |  |

Figure 2：Screenshot of conceptnet webpage．Source：conceptnet．io

## Problems：

－Newer and rarer words not well covered．

## N -grams



Figure 3: Screenshot of Google's N-gram webpage. Source: https://books.google.com/ngrams/.

## Problems:

- Relations one can infer statistically are limited.

You shall know a word by the company it keeps.
J.R. Firth, 1957

This is a sentence.
$\Rightarrow$ (this, is) (is, a) (a, sentence)
for word in sentence:
take the current_word_vector predict the next word
if prediction vector not next_word_vector:
(i.e. if the prediction wrong)
do gradient descent
repeat epoch times

## Architecture



Figure 4: Architecture network used in the simple w2v-algorithm.

Effectively a 2-layer NN without activation function and cross entropy loss:

$$
v_{l}\left(w_{t}\right)^{T} \cdot v_{O}\left(w_{t+1}\right)=v_{\text {prediction }} \rightarrow p\left(w_{t}\right):=\operatorname{softmax}\left(v_{\text {prediction }}\right)
$$

## Extract vocabulary and sentences using NLTK

```
import nltk
# OMT: First read the files as a big string into self.text
nltk.download('punkt')
# Separate self.text per sentence into list of strings
self.sents = nltk.sent_tokenize(self.text)
# Extract the unique vocabulary
self.vocab = nltk.word_tokenize(self.text)
self.vocab = [x.lower() for x in self.vocab]
self.vocab = list(set(self.vocab))
```


## Assign context to words

```
inps = []
outs = []
for sent in self.sents:
    sent = nltk.word_tokenize(sent)
    for i in range(len(sent)-1):
        # current input word
        word = sent[i]
        wordID = self.vocab.index(word.lower())
        inps.append(wordID) # sparse!
        # its corresponding context
        cntxt = sent[i+1]
        cntxtID = self.vocab.index(cntxt.lower())
        outs.append(cntxtID)
# The input data for the NN is inps whereby the i-th element
# has the i-th element of outs as corresponding label
# (in NN terms).
```

Increasing context window gives two possibilities:

- Predict target word from context (CBOW).
- Predict context from target word (Skip-gram).


## Continuous Bag-of-words

Predict target word from context words as input.


Avg. sum

Projection Layer


Output Layer

v

$$
\mathbf{v}_{\text {lnput }}=\frac{1}{|C|} \sum_{c \in C} \mathbf{v}_{c}
$$

## Skip-gram

## Predict context words from target word as input.



Figure 5: Image taken from http://mccormickml.com/assets/word2vec/training_data.png (27.5.2017).

## Comparison

Computational costs:

- CBOW

$$
O \propto(|C| \times d+d \times V)
$$

- Skip-gram

$$
O \propto|C| \times(d+d \times V)
$$

Which one to use:

- CBOW is faster and better for frequent words.
- Skip-gram good with smaller corpus and rarer words.


## N -grams

Extend vocabulary with ngrams
[New, York, Times] $\rightarrow$ [New, York, New York, Times, New York Times]

Introduce bigram score:

$$
\operatorname{score}\left(w_{i}, w_{j}\right)=\frac{\operatorname{count}\left(w_{i} w_{j}\right)-\delta}{\operatorname{count}\left(w_{i}\right) \times \operatorname{count}\left(w_{j}\right)},
$$

with discount coefficient $\delta$ (prevent infrequent n -grams).

- For n-grams run the bigram score multiple times.


## Subsampling



Figure 6: Image taken from http://mccormickml.com/assets/word2vec/training_data.png (27.5.2017).

$$
\Rightarrow \text { The is meaningless. }
$$

## Subsampling

Probability to remove/subsample:

$$
P\left(w_{i}\right)=\left(\sqrt{\frac{z\left(w_{i}\right)}{0.001}}+1\right) \frac{0.001}{z\left(w_{i}\right)} \approx \frac{1}{\sqrt{z\left(w_{i}\right)}},
$$

with $z\left(w_{i}\right)$ the relative frequency of the word.

- Only subsample words with frequency $\geq 0.26 \%$.
- The frequent word does not appear in context windows.
- Deleting the window means up to $4|C|$ less training data.


## Negative Sampling

- Gradient descent trains every weight based on one data tuple.
- Push one value to one and others to zero.
- Update only positive word and subset of negative words.
- 5-20 words for smaller and 2-5 for large datasets.
- For usual corpora: $\leq 0.1 \%$ of weights!


## Negative Sampling

In the code that means:

- Associate probability to each word given by

$$
P\left(w_{i}\right)=\frac{f\left(w_{i}\right)^{3 / 4}}{\sum\left(f\left(w_{j}\right)^{3 / 4}\right)}
$$

- Create array of size 100 M .
- Enter each word $P\left(w_{i}\right) \times 100 M$ times.
- Select random item from table.
$\Rightarrow$ Frequent words get corrected more frequently.
import gensim.models.KeyedVectors as kv

```
model = './GoogleNews-vectors-negative300.bin'
wordv = kv.load_word2vec_format( model, fbinary=True)
print('What is your base vector?')
positive1 = input()
print('What is the vector you want to substract?')
negative = input()
print('What is the vector you then want to add?')
positive 2 = input()
```

print('The most similar vector to this corresponds to: \n ')
print(wordv.most_similar(positive=[positive1, positive2],
negative=[negative]))

Thank you for your attention.

